Homework \#9
Due: 4/23/18

1. (20) Text question 11.70 .
2. (20) Calculate the maximum packing factor and corresponding weight fraction of fine particles in a bimodal mixture of monosized particles, $100 \mu \mathrm{~m}$ and $1 \mu \mathrm{~m}$ in diameter, and of the same material. Assume the large particles exhibit simple cubic packing and the fine particles exhibit loose random packing. Assume $V_{0}=1.0$.
3. (30) Powder compacts were uniaxially pressed in a cylindrical die of 13 mm diameter at varying levels of applied force. The compact height and mass was measured after pressing as compiled in the table below. (a) Calculate and plot the mean relative density (\%) for the level of applied pressure ( MPa ). Explain trends in the data. (b) Fit the data with the empirical model given in lecture, $\rho=\rho_{\mathrm{o}}+A \cdot \log (P)$ where $\rho$ is the relative density, $P$ is the applied pressure and $\rho_{\mathrm{o}}$ and $A$ are constants. (c) Propose a model that would fit the data better.

| Applied <br> Force <br> $(\mathrm{lbs})$ | Compact <br> Height <br> $(\mathrm{mm})$ | Compact <br> Mass <br> $(\mathrm{g})$ |  | Applied <br> Force <br> $(\mathrm{lbs})$ | Compact <br> Height <br> $(\mathrm{mm})$ | Compact <br> Mass <br> $(\mathrm{g})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 500 | 2.51 | 0.501 |  | 5000 | 1.96 | 0.492 |
| 500 | 2.52 | 0.507 |  | 5000 | 1.98 | 0.502 |
| 500 | 2.50 | 0.496 |  | 7500 | 1.91 | 0.494 |
| 500 | 2.50 | 0.496 |  | 7500 | 1.88 | 0.487 |
| 1000 | 2.43 | 0.494 |  | 7500 | 1.91 | 0.493 |
| 1000 | 2.45 | 0.495 |  | 7500 | 1.89 | 0.491 |
| 1000 | 2.47 | 0.499 |  | 10000 | 1.86 | 0.500 |
| 1000 | 2.45 | 0.493 |  | 10000 | 1.86 | 0.494 |
| 3000 | 2.17 | 0.495 |  | 10000 | 1.85 | 0.490 |
| 3000 | 2.15 | 0.491 |  | 10000 | 1.85 | 0.492 |
| 3000 | 2.18 | 0.494 |  | 15000 | 1.73 | 0.490 |
| 3000 | 2.16 | 0.493 |  | 15000 | 1.71 | 0.488 |
| 5000 | 1.97 | 0.495 |  | 15000 | 1.74 | 0.492 |
| 5000 | 1.96 | 0.494 |  | 15000 | 1.72 | 0.489 |

4. (30) An alumina powder having an average particle size of $1.6 \mu \mathrm{~m}$ is dry-pressed in a die, producing a 2 cm diameter x 2 cm high cylindrical compact having a mass of 12.75 g . The theoretical density of alumina is $3.97 \mathrm{~g} / \mathrm{cm}^{3}$. (a) Calculate the packing density of the as-pressed compact. (b) Upon firing, the compact densifies uniformly to a relative bulk density of 0.81 . Calculate the diameter (or height) of the fired cylinder. (c) Suggest two changes in process variables or material characteristics that would help achieve a higher fired density and explain why.
